



Optical potentials and nucleon scattering from ab-initio Green function

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**workshop on
Progress in Ab Initio Techniques in Nuclear Physics
TRIUMF, 28 Feb – 3 Mar**

Idea

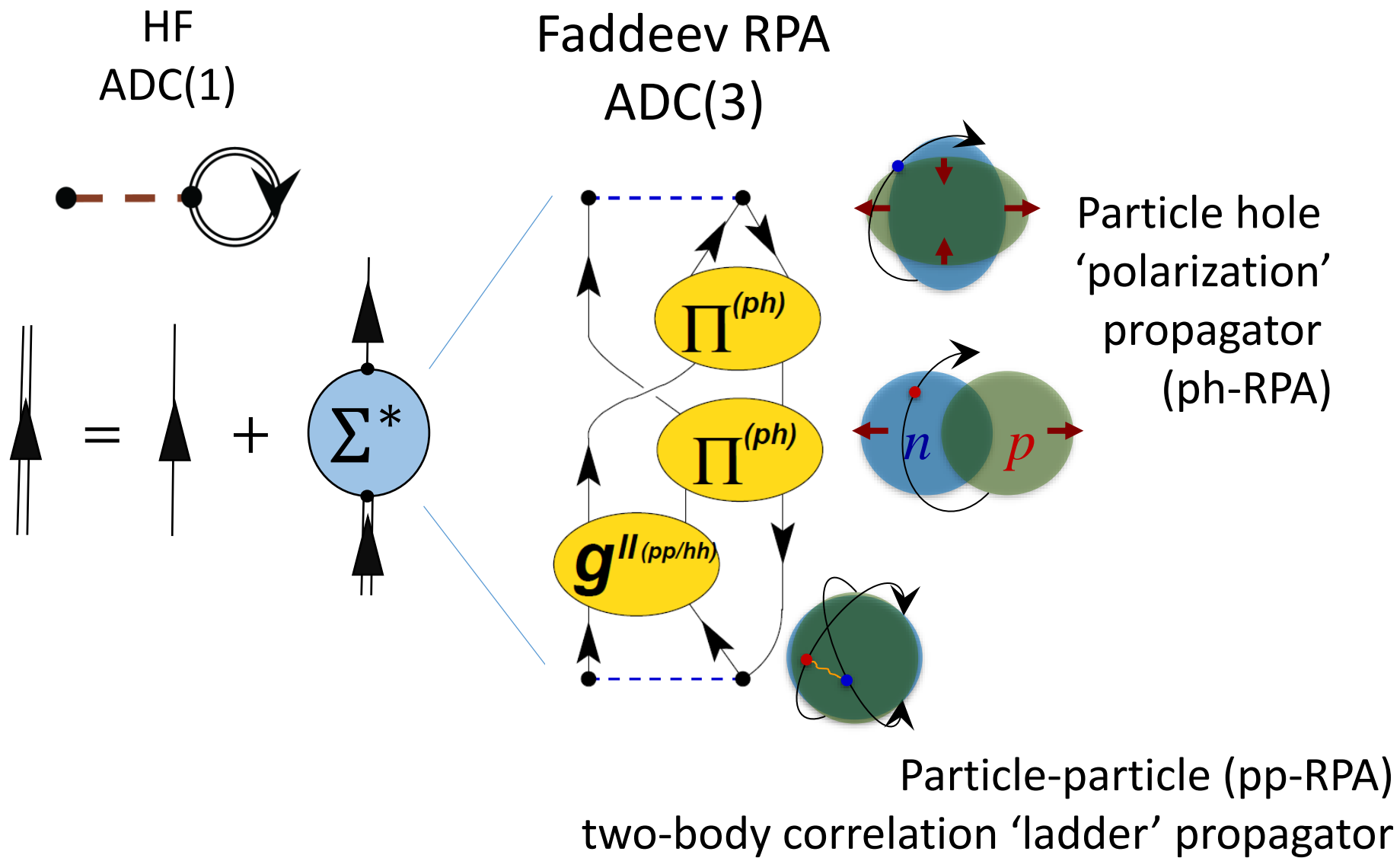
Objective: an effective, consistent description of structure and reactions with a single formalism.

(Hopefully) Predictive power of nuclear reactions measurements over a range of exotic isotopes.

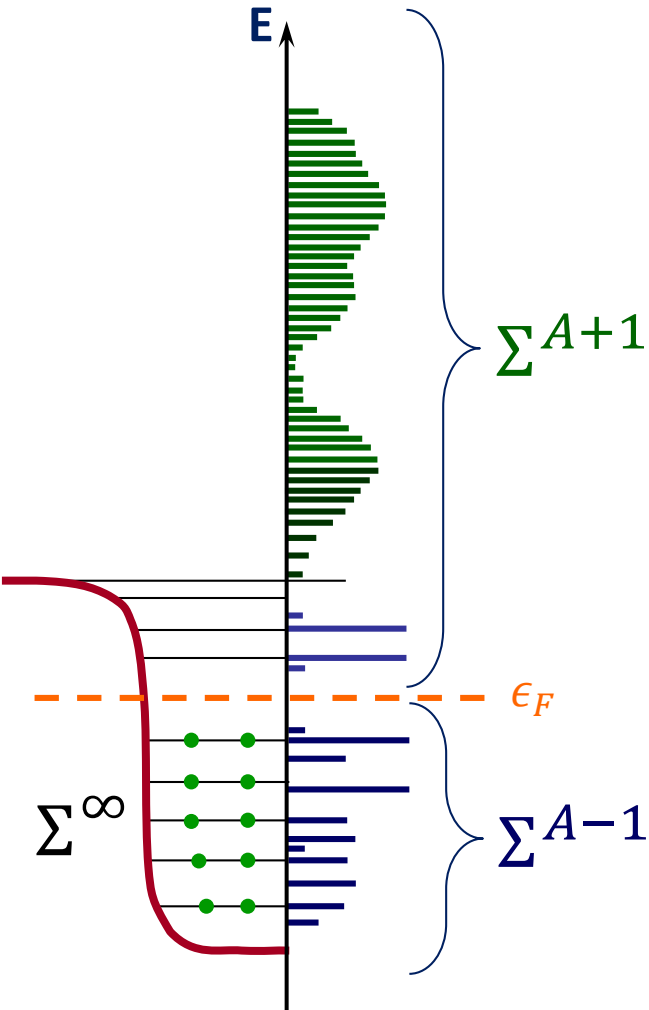
Method: Optical potential derived from Self Consistent Green Function and χ EFT interactions.

1. reproduce nuclear bulk properties, i.e. binding energy and radii;
NNLO_{sat}
2. use the same description to consistently generate an optical potential reproducing elastic scattering data.

Green Functions (*Dyson Equation*)

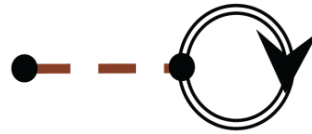


Nucleon elastic scattering

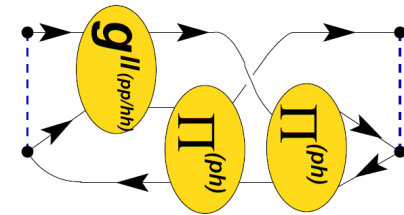


The irreducible self-energy is a nucleon-nucleus optical potential*

$$\Sigma^*(\mathbf{r}, \mathbf{r}'; \varepsilon) = \underbrace{\Sigma_{\alpha\beta}^{\infty}}_{\text{mean-field}} - \frac{1}{\pi} \int_{\varepsilon_F}^{\infty} dE' \frac{\text{Im} \Sigma^*(\mathbf{r}, \mathbf{r}'; E')}{\varepsilon - E' + i\eta} + \frac{1}{\pi} \int_{-\infty}^{\varepsilon_F} dE' \frac{\text{Im} \Sigma^*(\mathbf{r}, \mathbf{r}'; E')}{\varepsilon - E' - i\eta}$$



resonances beyond mean-field



➔ This provides *consistent* many-body and scattering wave functions

*Mahaux & Sartor, Adv. Nucl. Phys. 20 (1991), Escher & Jennings PRC66:034313 (2002)

- Solve Dyson equation in HO Space, find $\Sigma_{n,n'}^{l,j^*}(E)$

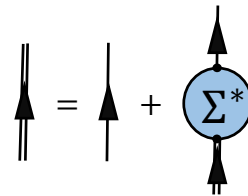


- diagonalize in full continuum momentum space $\Sigma^{l,j^*}(k, k', E)$

$$\frac{k^2}{2m} \psi_{l,j}(k) + \int dk' k'^2 \left(\Sigma^{l,j^*}(k, k', E) + V_{coul}(k, k') \right) \psi_{l,j}(k') = E \psi_{l,j}(k)$$



$$\Sigma_{n,n'}^{l,j^*}(E)$$

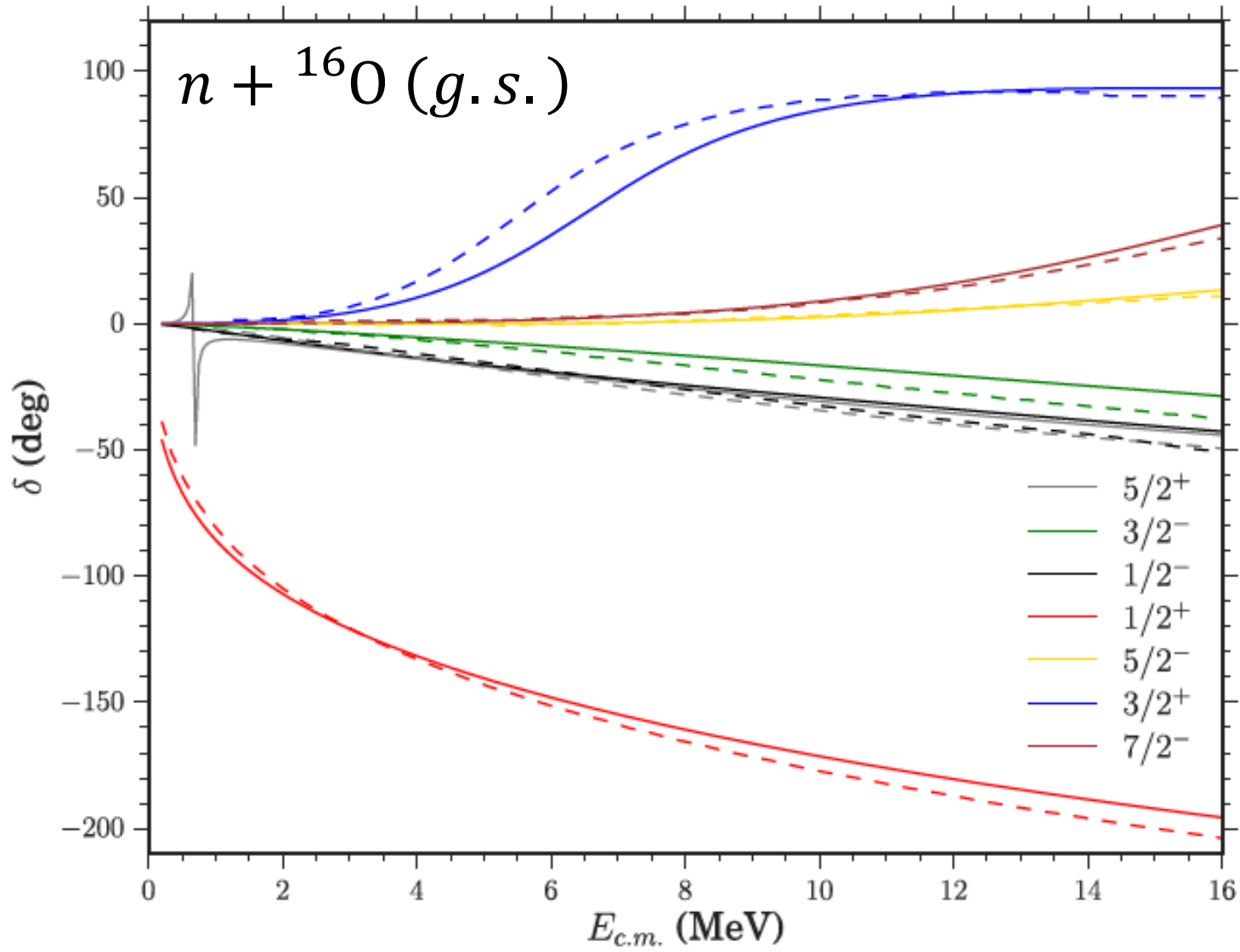


Freshly baked
RESULTS

[arXiv:1612.01478](https://arxiv.org/abs/1612.01478) [nucl-th]

SRG-N³LO, $\Lambda = 2.66 \text{ fm}^{-1}$

$n + {}^{16}\text{O} (g.s.)$



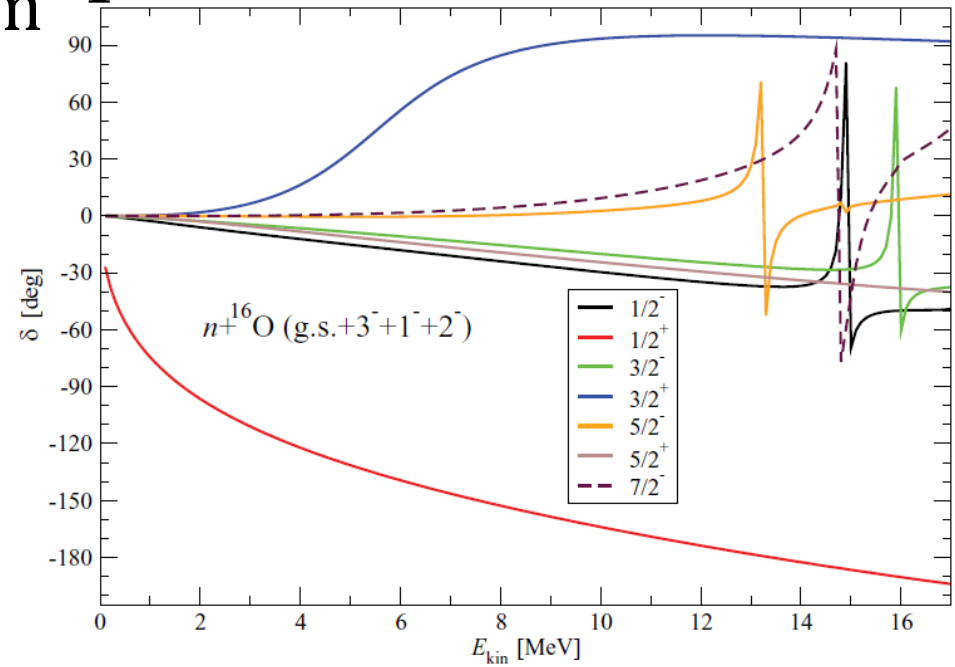
--- Navrátil, Roth, Quaglioni,
PRC82, 034609 (2010)

— Σ^∞

SRG-N³LO, $\Lambda = 2.66 \text{ fm}^{-1}$

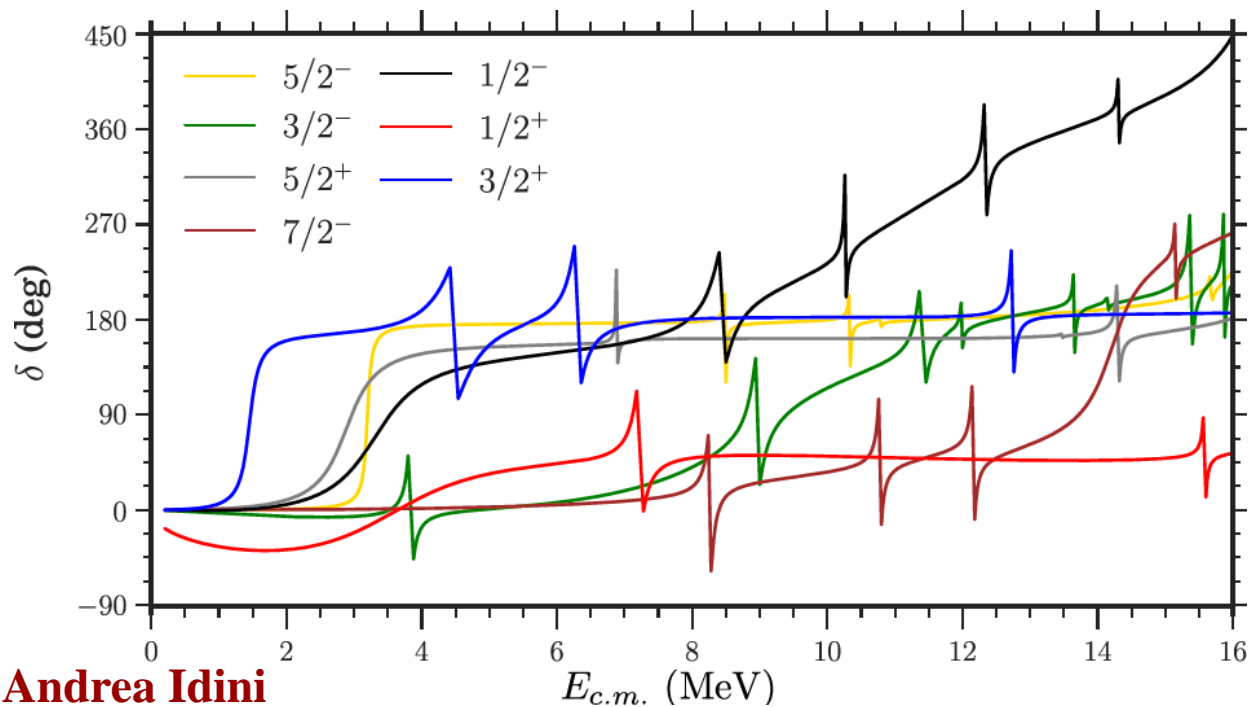
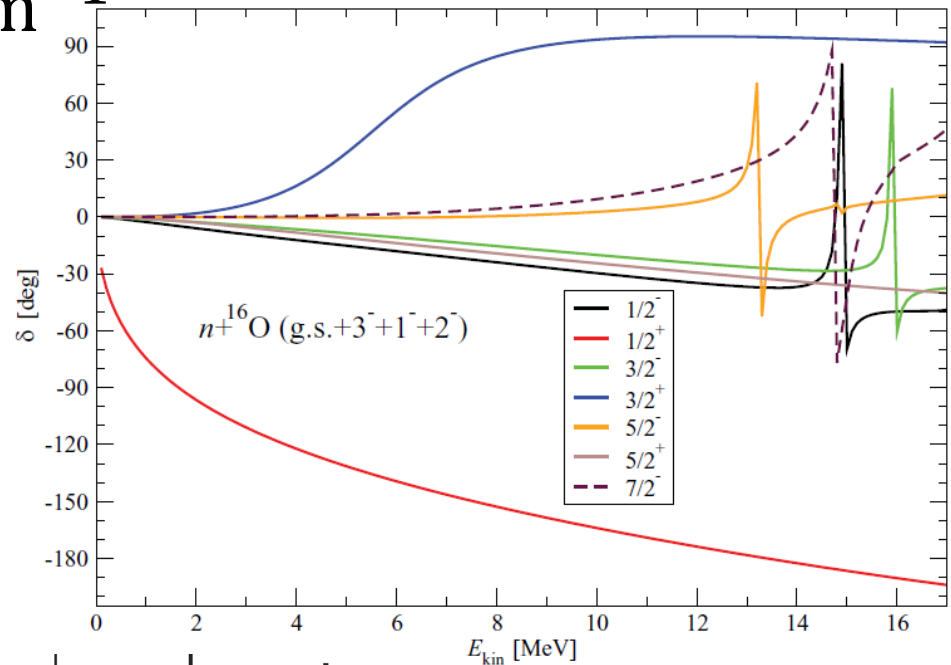
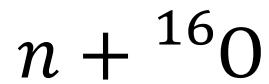
Navrátil, Roth, Quaglioni,
PRC82, 034609 (2010)

$n + {}^{16}\text{O}$



SRG-N³LO, $\Lambda = 2.66 \text{ fm}^{-1}$

Navrátil, Roth, Quaglioni,
PRC82, 034609 (2010)



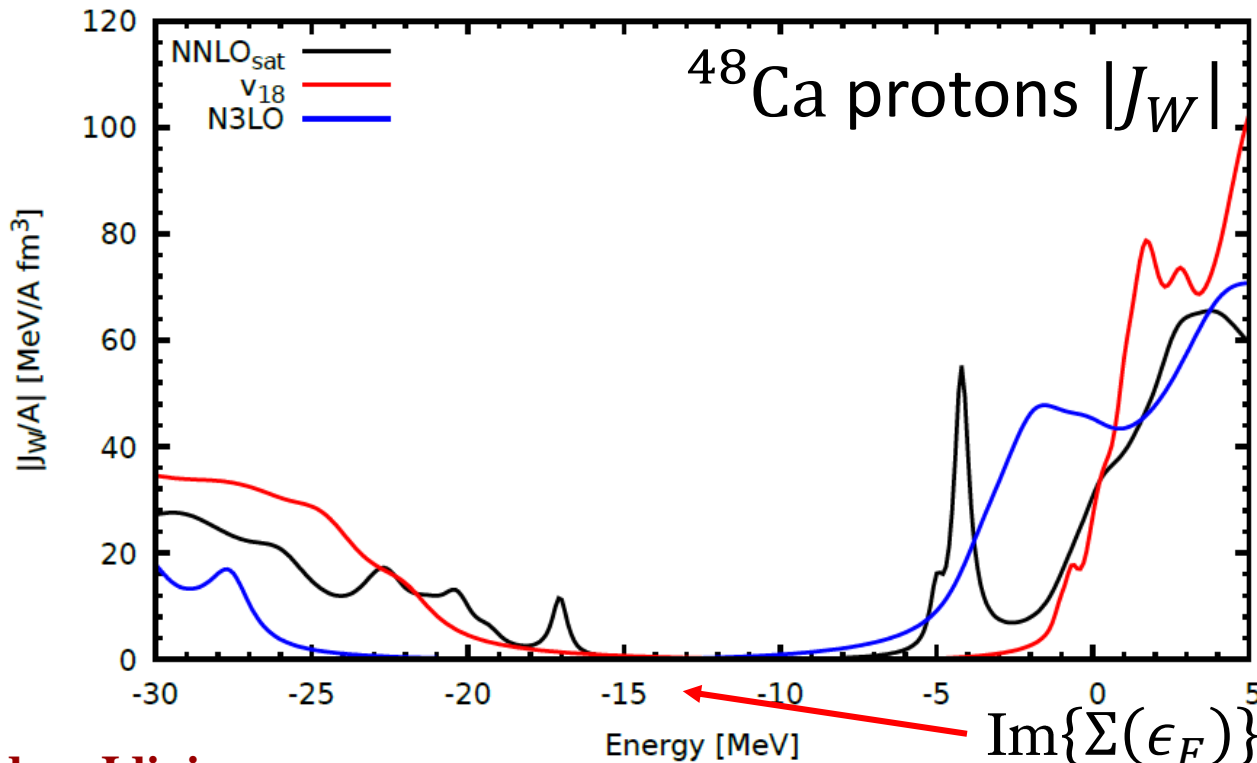
Volume integrals

$$J_W^\ell(E) = 4\pi \int dr r^2 \int dr' r'^2 \text{Im} \Sigma_0^\ell(r, r', E)$$

Non local potential

$$J_V^\ell(E) = 4\pi \int dr r^2 \int dr' r'^2 \text{Re} \Sigma_0^\ell(r, r'; E).$$

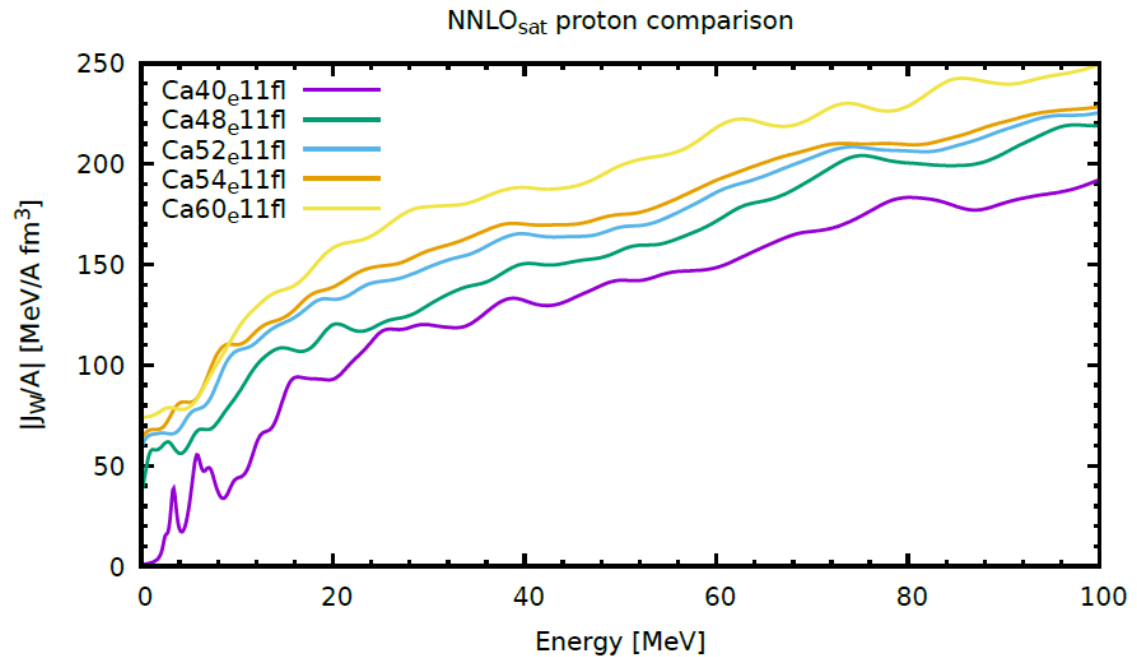
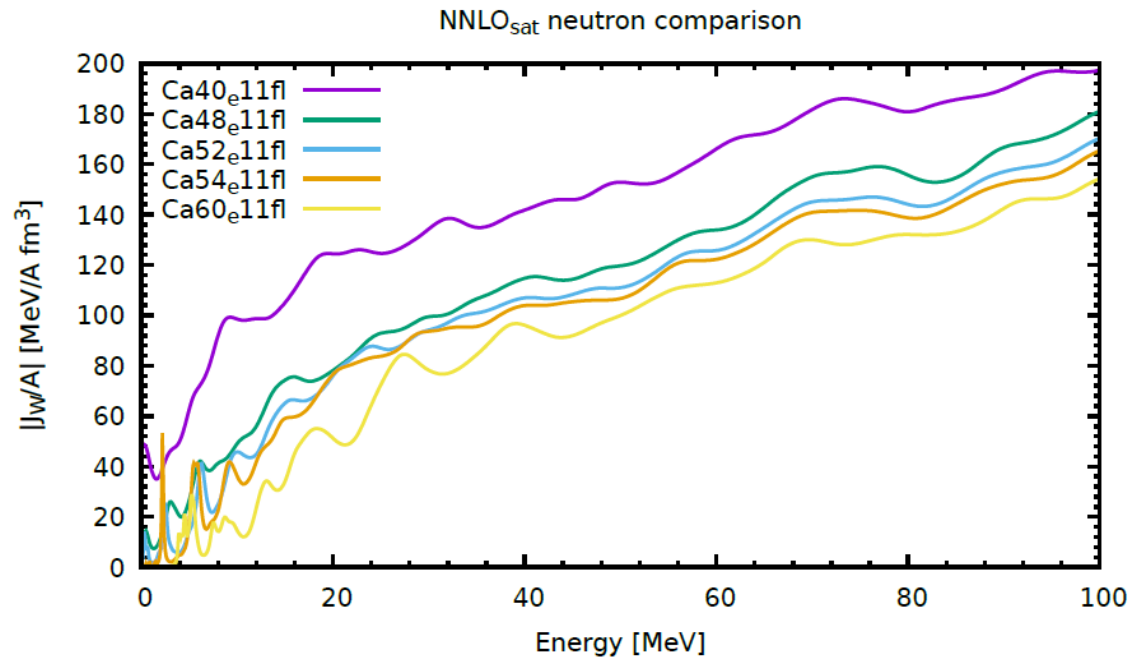
$$\tilde{\Sigma}_{n_a, n_b}^{\ell j}(E) = \sum_r \frac{m_{n_a}^r m_{n_b}^r}{E - \varepsilon_r \pm i\eta}$$

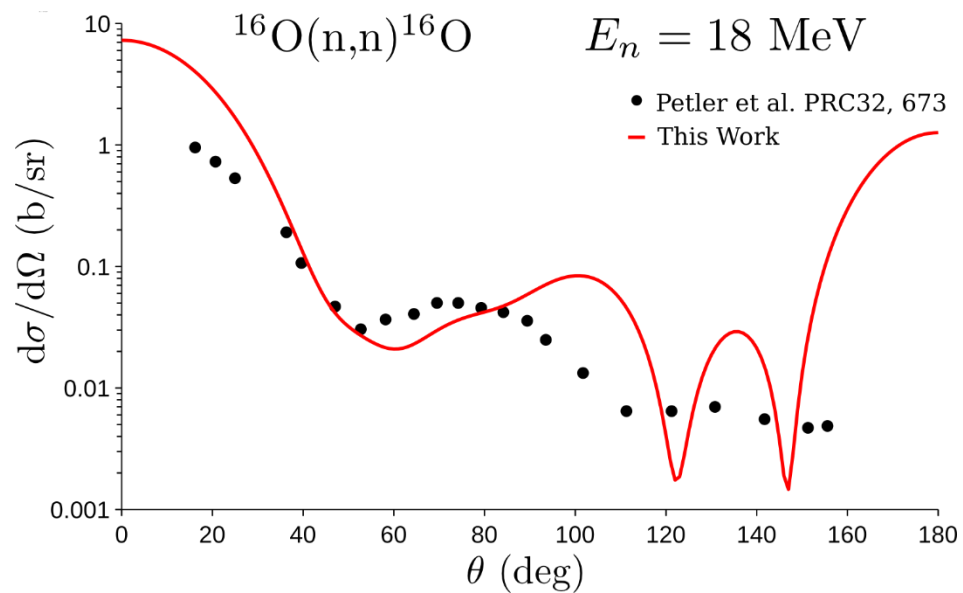
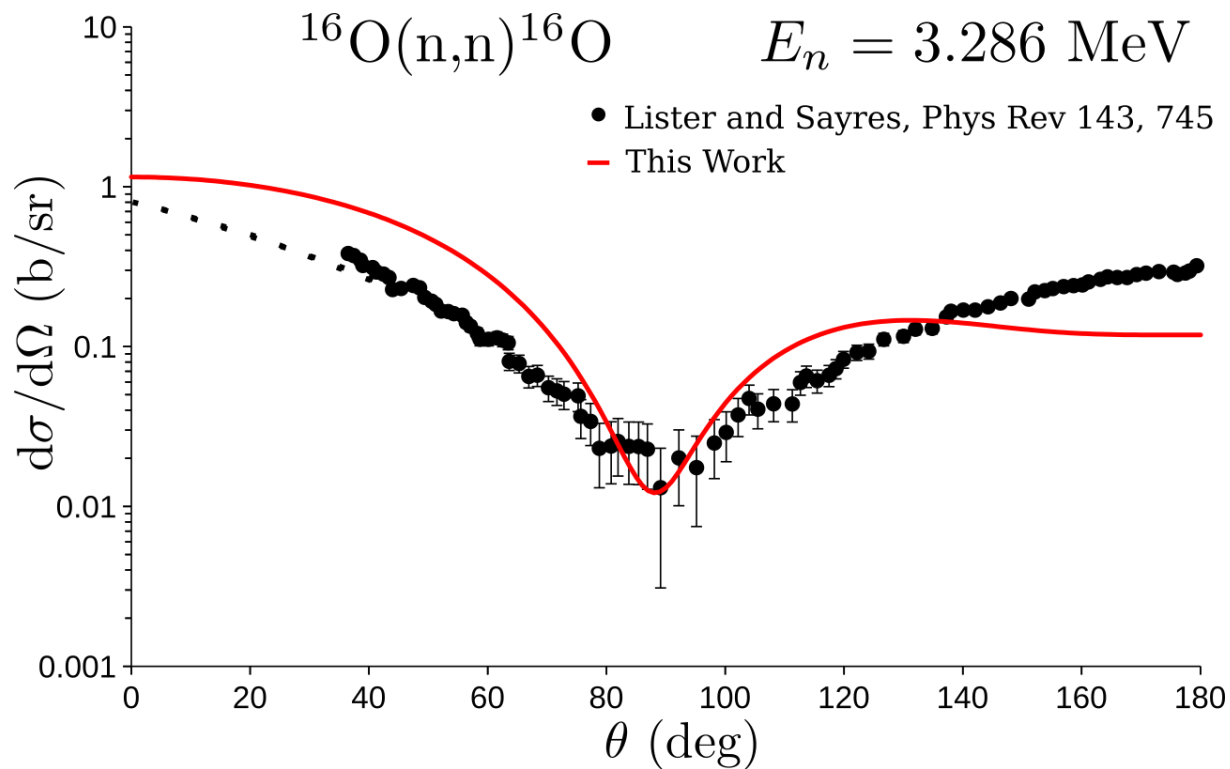


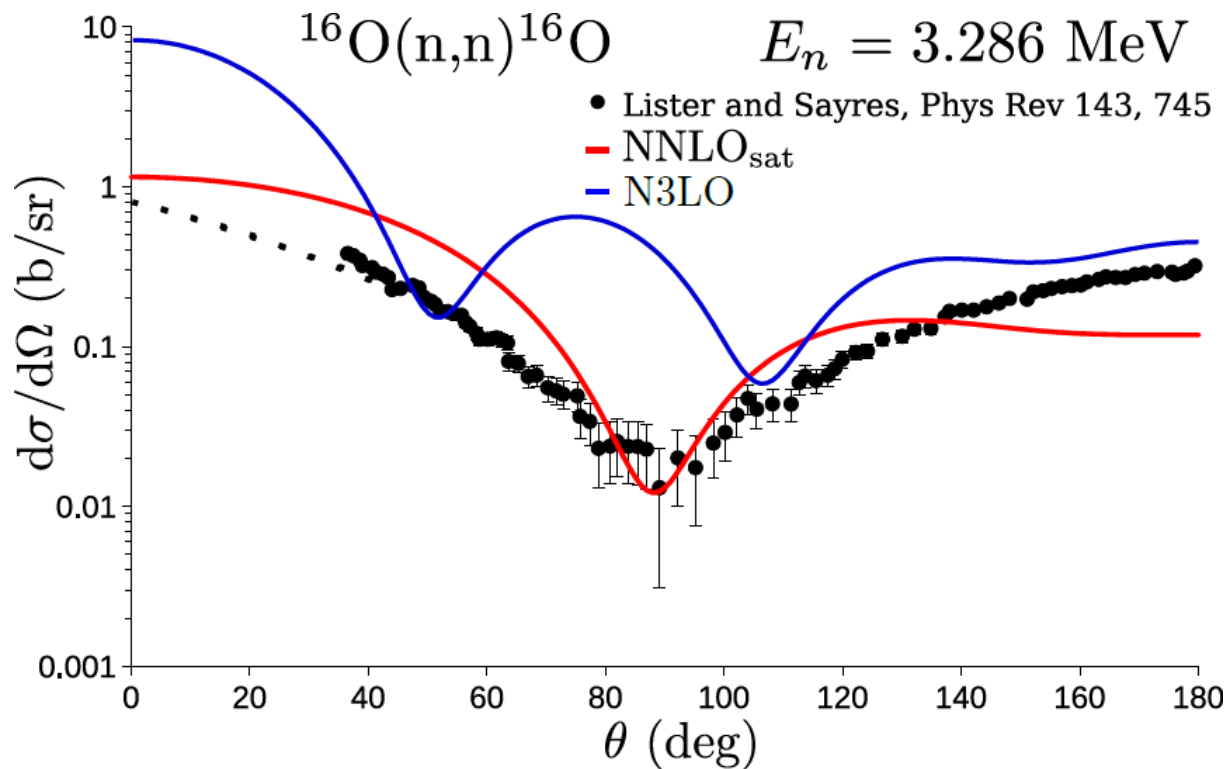
different Fermi energies and particle-hole gap for different interactions

Ca isotopes

neutron and proton
volume integrals of
self energies.





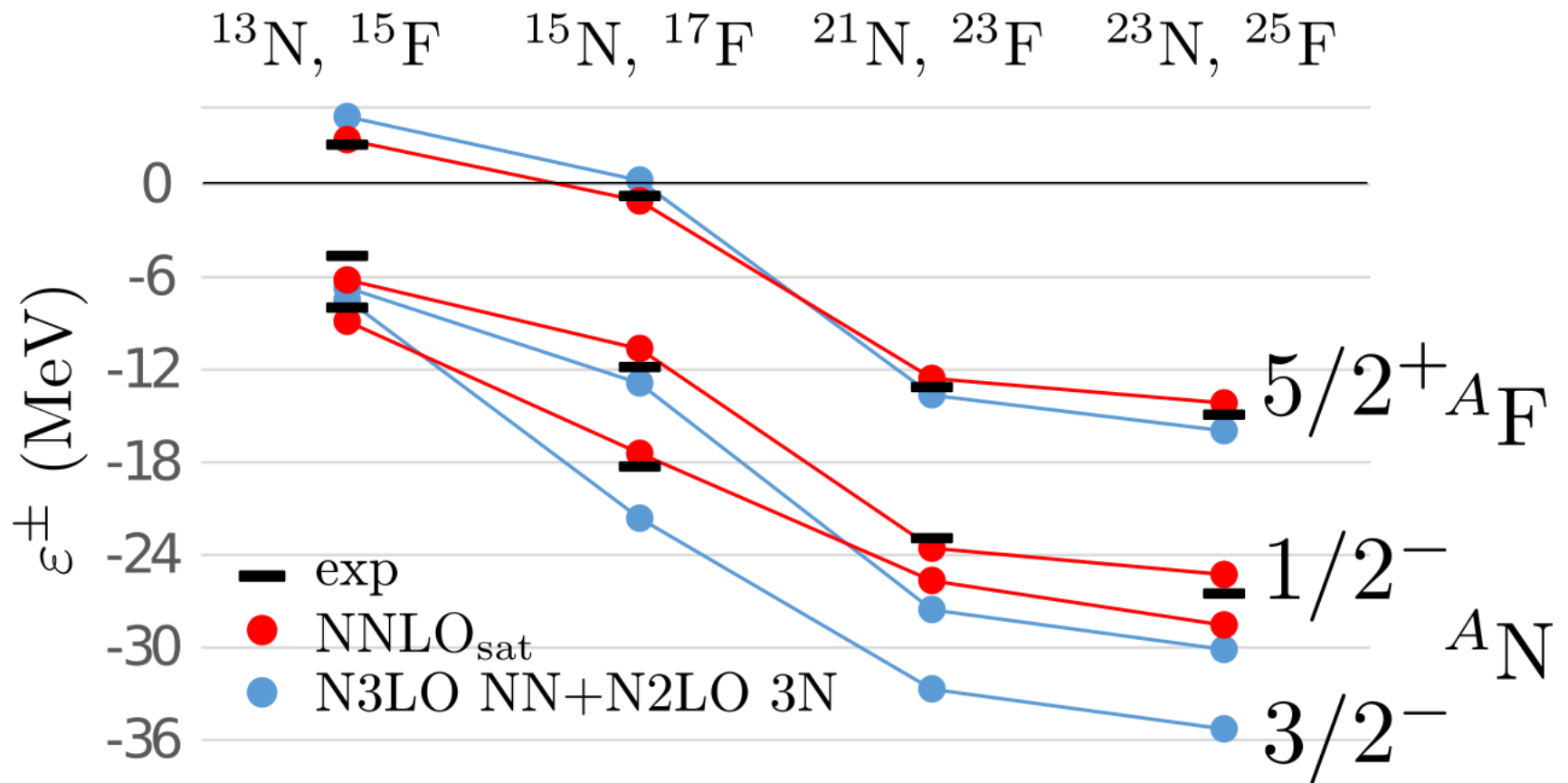
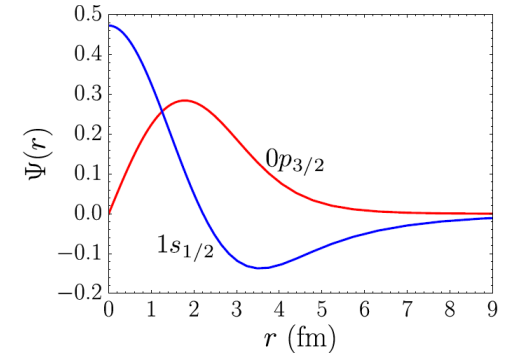


$^{16}\text{O} \langle r_p \rangle$

experiment	$2.699 \pm 0.005 \text{ fm}$
NNLO _{sat}	2.734 fm
N3LO NN	2.354 fm

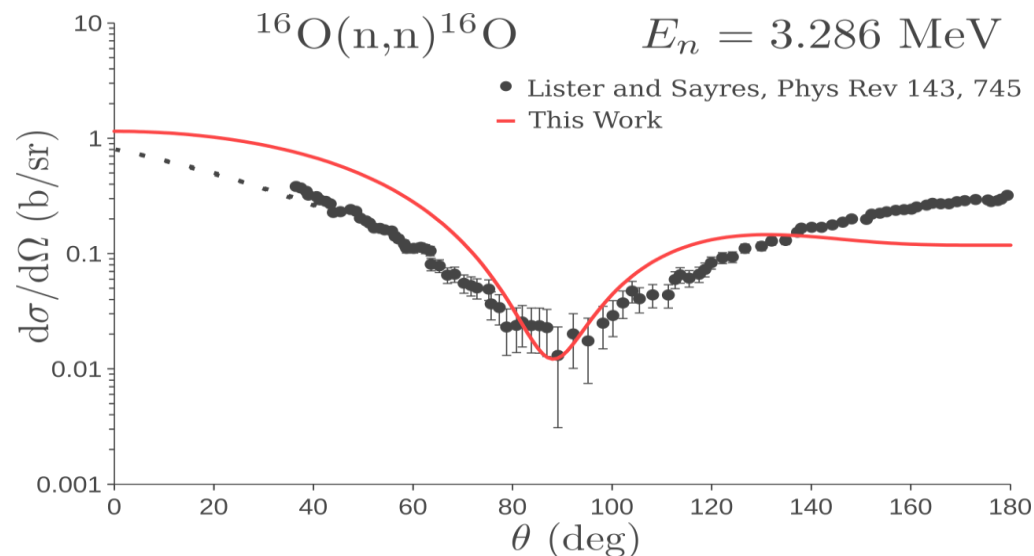
Overlap function

$$\Psi_i(r) = \sqrt{A} \int \prod_{i=1}^A dr_i \Phi_{(A-1)}^+(r_1, \dots, r_{A-1}) \Phi_{(A)}^+(r_1, \dots, r_A)$$



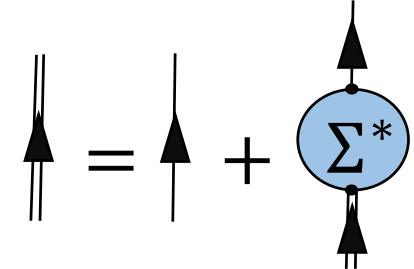
Conclusions and Perspectives

- We are developing an interesting tool to study nuclear reactions effectively.
We have defined a non-local generalized optical potential corresponding to nuclear self energy.
- This tool is useful to probe properties of nuclear interactions.
- *Radii, saturation and bulk properties are fundamental!*



Why Green's Functions?

Dyson Equation

$$g_{\alpha\beta}(\omega) = g_{\alpha\beta}^0(\omega) + \sum_{\gamma\delta} g_{\alpha\gamma}^0(\omega) \Sigma_{\gamma\delta}^*(\omega) g_{\delta\beta}(\omega)$$


Equation of motion

$$\left(E + \frac{\hbar^2}{2m} \nabla_r^2 \right) G(\mathbf{r}, \mathbf{r}'; E) - \int d\mathbf{r}'' \Sigma(\mathbf{r}, \mathbf{r}''; E) G(\mathbf{r}'', \mathbf{r}'; E) = \delta(\mathbf{r} - \mathbf{r}').$$

Corresponding Hamiltonian

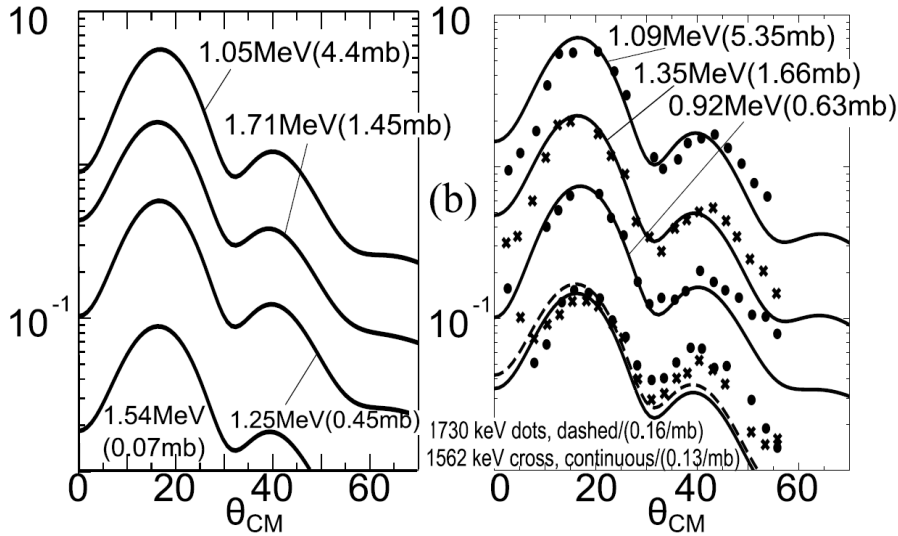
$$\mathcal{H}_{\mathcal{M}}(\mathbf{r}, \mathbf{r}') = -\frac{\hbar^2}{2m} \nabla_r^2 \delta(\mathbf{r} - \mathbf{r}') + \Sigma(\mathbf{r}, \mathbf{r}'; E + i\epsilon)$$

Σ corresponds to the Feshbach's generalized optical potential

Why optical potentials?

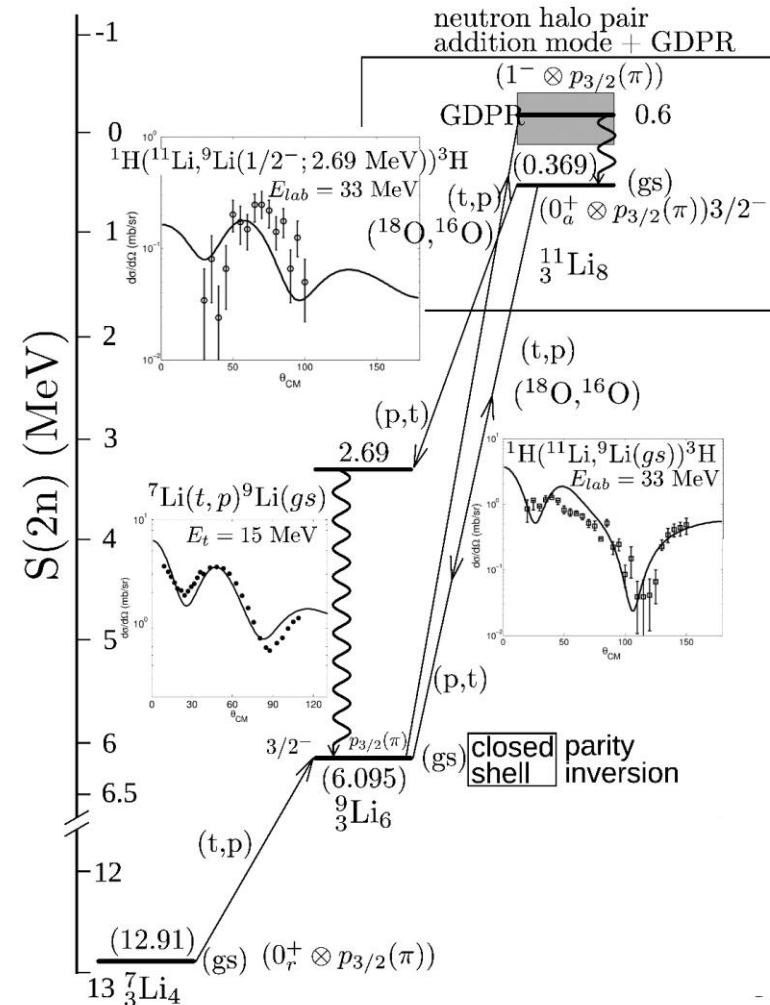
- Optical potentials **reduce many-body complexity** decoupling structure contribution and reactions dynamics.

1 particle transfer

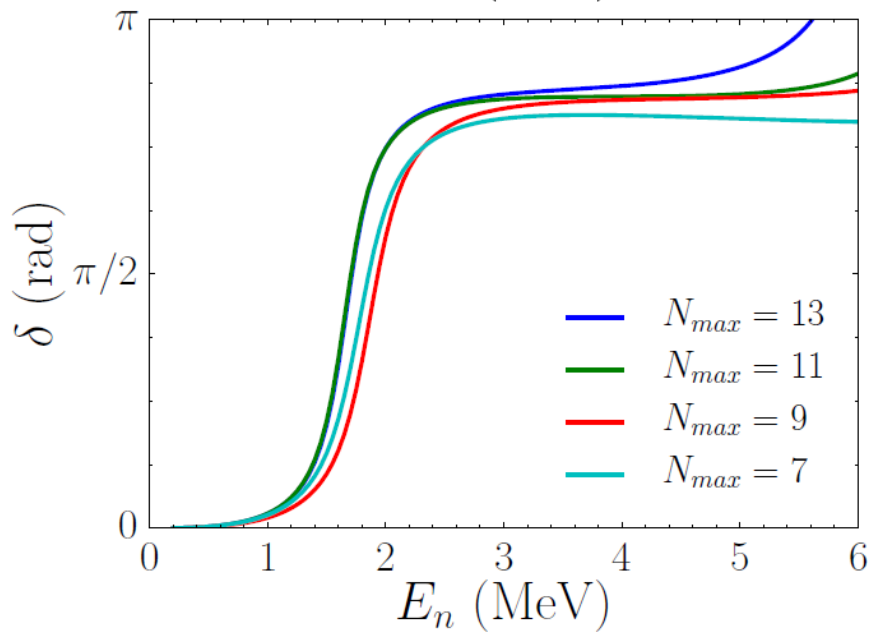
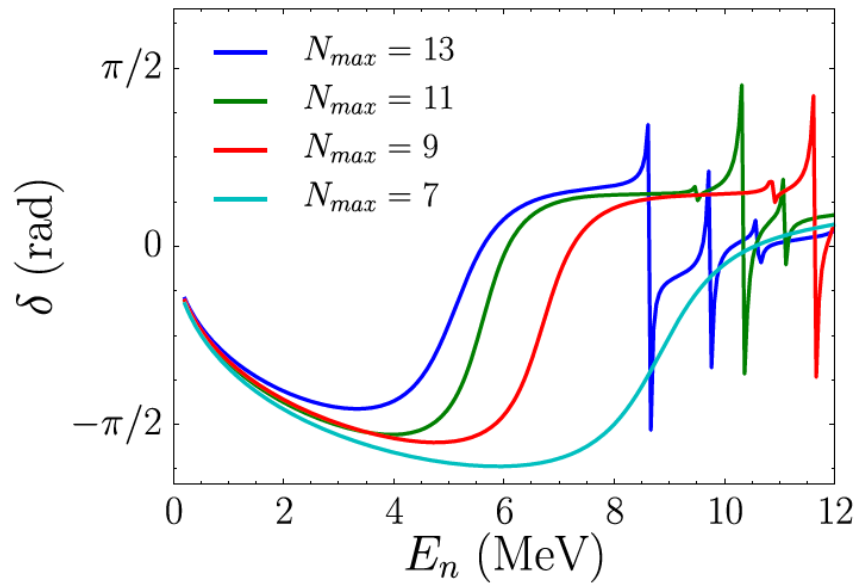


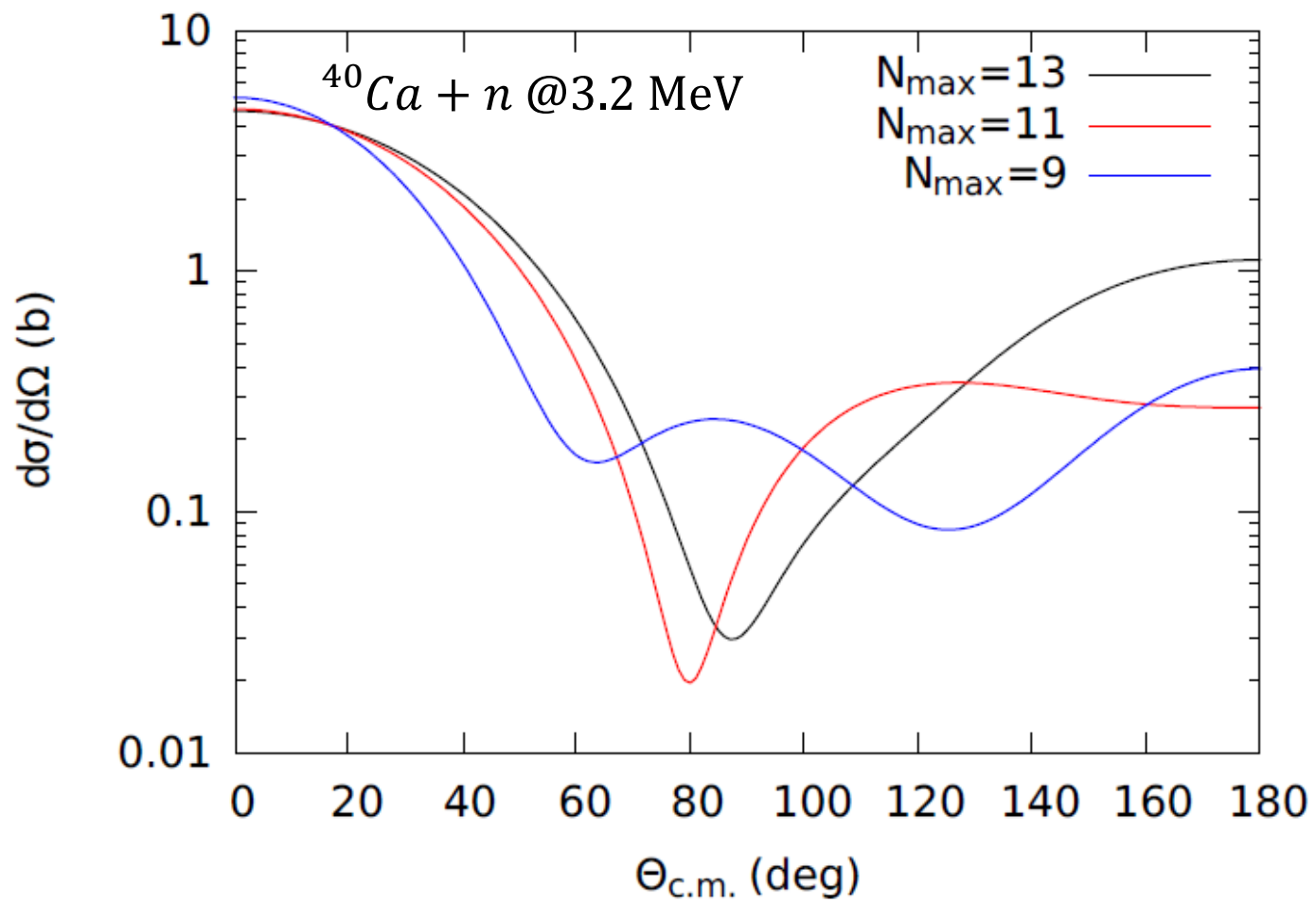
A.I. et al. *Phys. Rev. C* **92**, 031304 (2015)

2 particle transfer



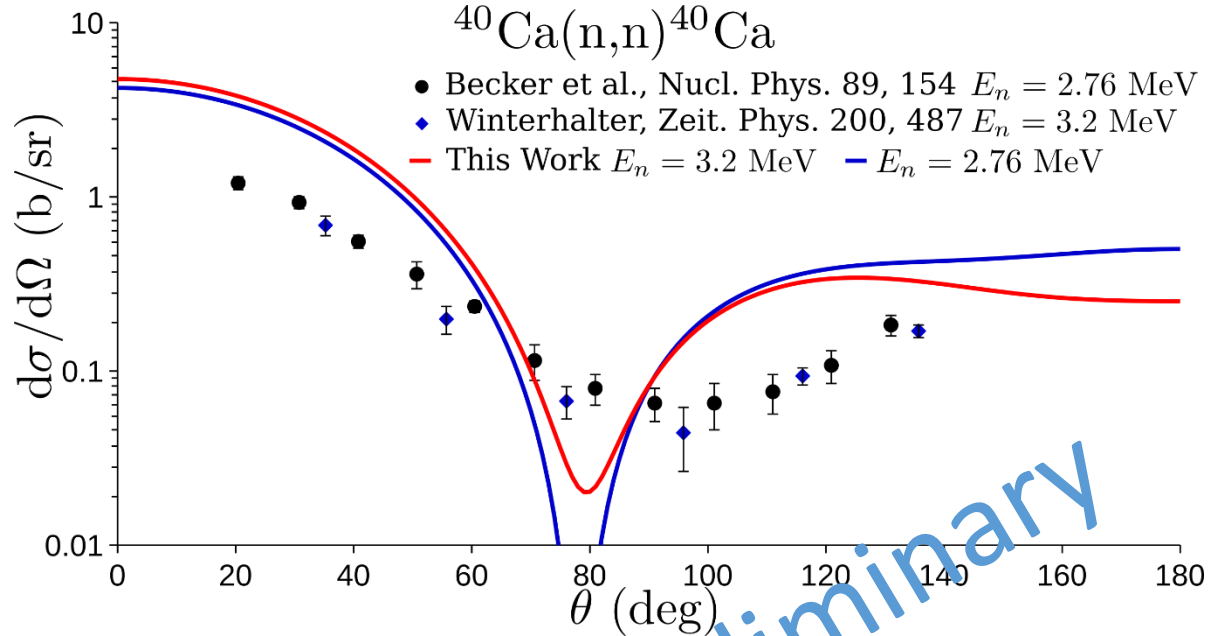
Broglia et al. *Phys. Scr.* **91** 06301* (2016)



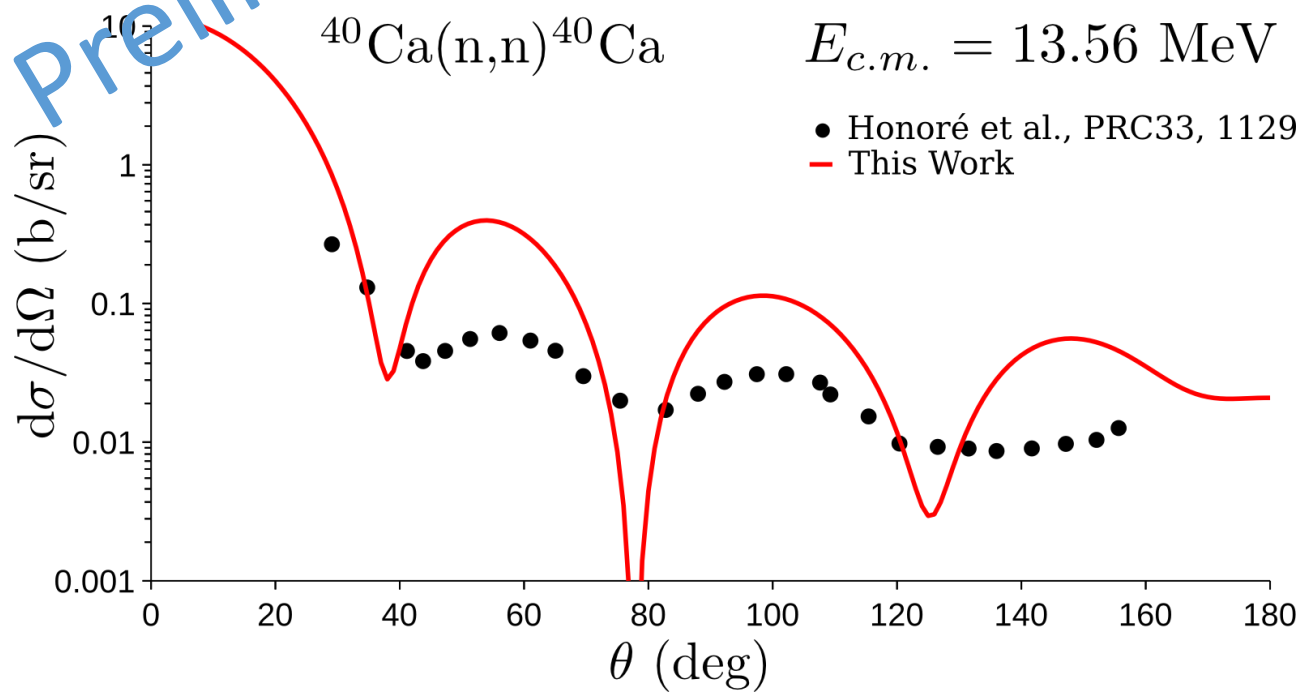


$^{40}\text{Ca}(n,n)^{40}\text{Ca}$

- Becker et al., Nucl. Phys. 89, 154 $E_n = 2.76$ MeV
- ◆ Winterhalter, Zeit. Phys. 200, 487 $E_n = 3.2$ MeV
- This Work $E_n = 3.2$ MeV — $E_n = 2.76$ MeV

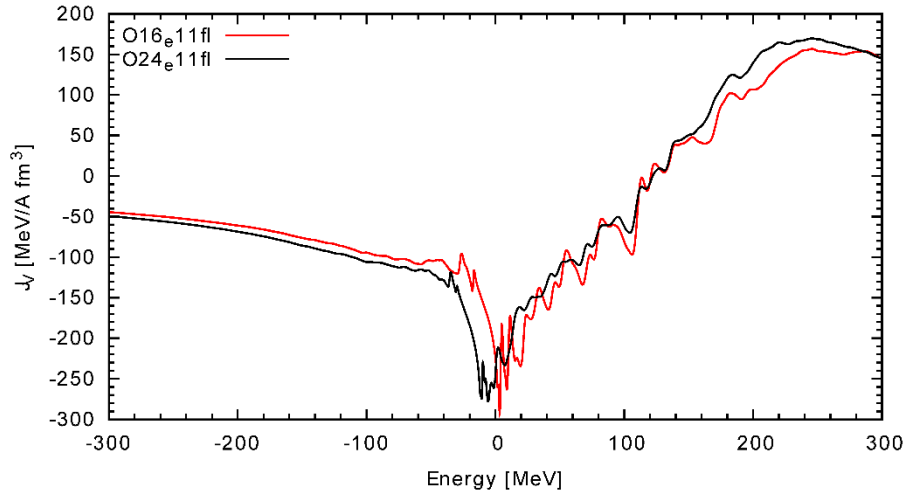
 $^{40}\text{Ca}(n,n)^{40}\text{Ca}$ $E_{c.m.} = 13.56$ MeV

- Honoré et al., PRC33, 1129
- This Work

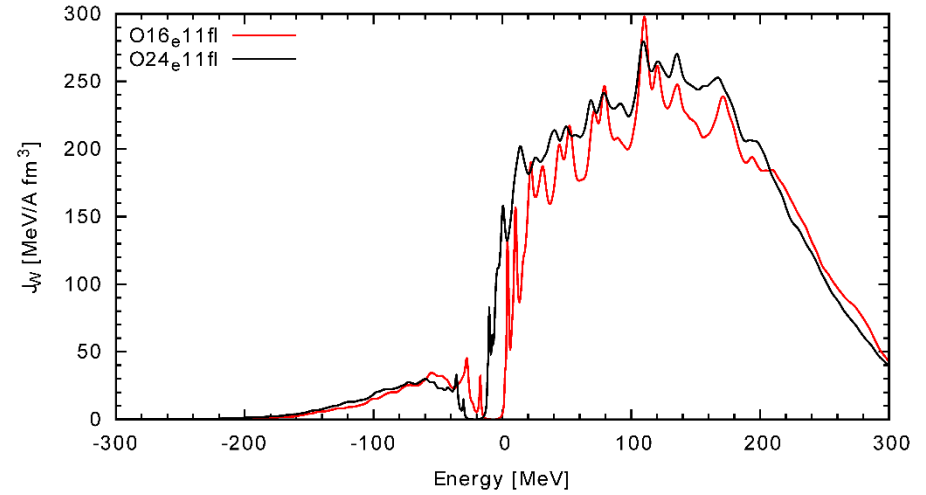


^{16}O and ^{24}O

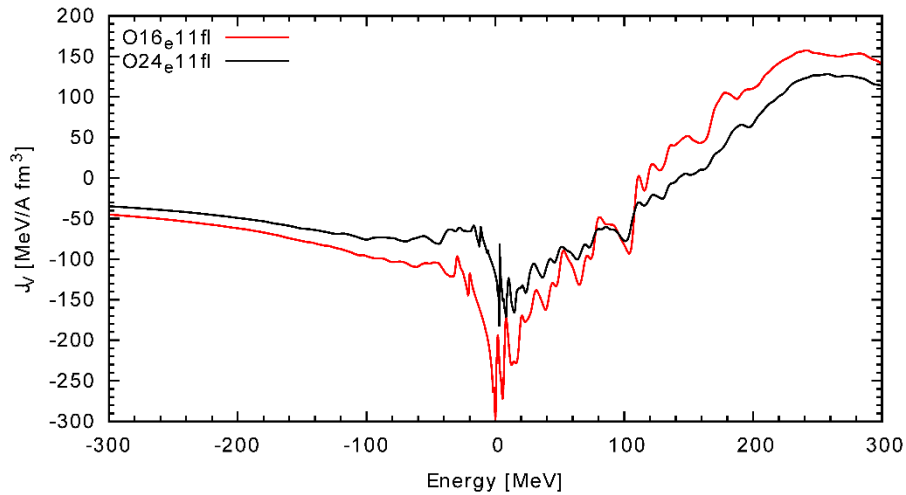
NNLO_{sat} proton comparison



NNLO_{sat} proton comparison



NNLO_{sat} neutron comparison



NNLO_{sat} neutron comparison

